Calculus II, Section K<br>Quiz \# 11<br>November 19th 2008<br>20 minutes

First Name : $\qquad$
Last Name : $\qquad$

1. Let $\mathbf{v}=\left[\begin{array}{r}1 \\ -1 \\ 1\end{array}\right]$.
(a) Give the matrix $P$ of the orthogonal projection onto the space spanned by $\mathbf{v}$.
(Give results here and use the back pages for your calculations)

$$
P=
$$

(b) Give the matrix $P_{\perp}$ of the orthogonal projection onto the subspace orthogonal to $\mathbf{v}$.
(Give results here and use the back pages for your calculations)

$$
P_{\perp}=
$$

2. Let $A=\left[\begin{array}{rrr}1 & -1 & 0 \\ -1 & 0 & 1 \\ 0 & 1 & -1\end{array}\right]$.
(a) Give a basis for $\operatorname{Im}(A)$
(Give results here and use the back pages for your calculations)
(b) Give an orthonormal basis for $\operatorname{Im}(A)$
(Hint : use the Gram-Schmidt procedure)
(Give results here and use the back pages for your calculations)
(c) Give the $Q R$ factorization for $A$

$$
Q=\quad R=
$$

Use this page for your calculations

Use this page for your calculations

