Calculus II, Section K Quiz \# 7<br>October 15th 2008

First Name : $\qquad$
Last Name : $\qquad$

1. Give an equation for the line passing through the points $\mathbf{p}_{0}=\left[\begin{array}{l}2 \\ 1\end{array}\right]$ and $\mathbf{p}_{1}=\left[\begin{array}{r}1 \\ -1\end{array}\right]$. (Give results here and use the back pages for your calculations)
2. Find a one-to-one parametrization for the plane passing though the points $\mathbf{p}_{0}=\left[\begin{array}{l}2 \\ 0 \\ 1\end{array}\right], \mathbf{p}_{1}=\left[\begin{array}{r}-1 \\ 1 \\ -1\end{array}\right]$ and $\mathbf{p}_{2}=\left[\begin{array}{l}2 \\ 1 \\ 0\end{array}\right]$
(Give results here and use the back pages for your calculations)
3. In this question the image $S$ of the unit circle by the matrix $A=$ $\left[\begin{array}{cc}3 & -1 \\ -1 & 3\end{array}\right]$ will be studied.
(a) Give the equation of $S$
(Give results here and use the back pages for your calculations)
(b) Compute the maximum distance of a point of $S$ to the origin.
(Hint : write $x_{1}=\cos t, x_{2}=\sin t$ for the components of a vector $\mathbf{x}$, compute the vector $A \mathbf{x}$ and compute the square of its length, then maximize over $t$.)
(Give results here and use the back pages for your calculations)

## Maximal length $=$

4. Give the augmented matrix of the following system of linear equations:

$$
\begin{aligned}
x_{1}-x_{2}+x_{3}-x_{4} & =0 \\
2 x_{1}-2 x_{2}+3 x_{3}+x_{4} & =1 \\
-x_{1}+x_{2}+4 x_{3}+5 x_{4} & =6 \\
3 x_{1}-3 x_{2}+2 x_{3} & =0
\end{aligned}
$$

$$
[A \mid b]=
$$

Use this page for your calculations

