

GEORGIA TECH

SCHOOL OF MATHEMATICS

MATH 1502

## CALCULUS II, SECTION D

## Quiz # 1

August 26th 2009

First Name : -----

Last Name : -----

1. Compute the following limits (*what method are you using?*)

$$\lim_{x \rightarrow \pi/2} \frac{\cos^2 x}{1 - \sin^5 x} =$$

$$\lim_{x \rightarrow 0} \frac{\ln \cos x}{x^2} =$$

$$\lim_{n \rightarrow \infty} (n^2 + 2n)^{1/n} =$$

2. Is the following integral convergent or not? (*give the method of proof*)

$$\int_1^{+\infty} \frac{\ln^2 x}{x^2} dx$$

3. Give the set of values of  $\alpha$  for which the following integral converges?  
(*Hint : beware of the two limit points!*)

$$\int_0^{\infty} \frac{dx}{x^{1-\alpha}(1+x)}$$